Impedance Control Reduces Instability That Arises from Motor Noise

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There is ample evidence that humans are able to control the endpoint impedance of their arms in response to active destabilizing force fields. However, such fields are uncommon in daily life. Here, we examine whether the CNS selectively controls the endpoint impedance of the arm in the absence of active force fields but in the presence of instability arising from task geometry and signal-dependent noise (SDN) in the neuromuscular system. Subjects were required to generate forces, in two orthogonal directions, onto four differently curved rigid objects simulated by a robotic manipulandum. The endpoint stiffness of the limb was estimated for each object curvature. With increasing curvature, the endpoint stiffness increased mainly parallel to the object surface and to a lesser extent in the orthogonal direction. Therefore, the orientation of the stiffness ellipses did not orient to the direction of instability. Simulations showed that the observed stiffness geometries and their pattern of change with instability are the result of a tradeoff between maximizing the mechanical stability and minimizing the destabilizing effects of SDN. Therefore, it would have been suboptimal to align the stiffness ellipse in the direction of instability. The time course of the changes in stiffness geometry suggests that modulation takes place both within and across trials. Our results show that an increase in stiffness relative to the increase in noise can be sufficient to reduce kinematic variability, thereby allowing stiffness control to improve stability in natural tasks.

Introduction

Most tasks in daily life, from using a pencil, typing on a keyboard, or eating with a fork, involve dynamic interactions with the environment. Humans are dexterous at such interactions. However, in many cases, the geometry of the task makes the interaction inherently unstable (Rancourt and Hogan, 2001; Milner, 2002a; Franklin et al., 2003a). Rancourt and Hogan (2001) postulated that the control of the endpoint stiffness of the arm could play an important role in stabilizing such inherently unstable interactions. However, to change the endpoint stiffness, muscular coactivation is needed (Hogan, 1984; Milner and Cloutier, 1993; Milner, 2002b). Such muscle contraction increases internal variability as a result of signal-dependent motor noise (SDN) and could therefore add to any instability (Harris and Wolpert, 1998).

Studies have shown that subjects have a limited ability to control their endpoint stiffness cognitively (Gomi and Osu, 1998; Perreault et al., 2002). However, subjects do modulate stiffness in response to instability generated by robotic interfaces. For example, appropriate changes in stiffness have been seen when significant amounts of energy are added to the arm by either applying random force pulses while subjects maintain a fixed posture (Darainy et al., 2004) or creating a divergent force field in which deviations from a straight line movement are actively amplified (Burdet et al., 2001; Franklin et al., 2003b, 2004, 2007). In these studies, the destabilizing forces are either independent of hand position variability (Darainy et al., 2004) or increase linearly with hand deviation (Burdet et al., 2001; Franklin et al., 2003b, 2004, 2007), such that destabilizing force variability is proportional to positional variability. In contrast, when interacting with real-world objects that impose stability constraints (e.g., a screwdriver), the perturbing forces can increase supralinearly with positional errors. In this case, kinematic variability must be tightly controlled to maintain stability. It is unknown whether stiffness control is seen in such interactions in which instability arises from purely passive elements and noise in the motor commands. Theoretical work suggests that, if the stabilizing forces attributable to stiffness increase faster than the destabilizing forces attributable to SDN, then muscular coactivation will reduce kinematic variability and increase stability (Selen et al., 2005).

Here we examine whether subjects control the endpoint stiffness of their arm to maintain stability in a natural task. Subjects produced a force of defined magnitude and direction against objects of different curvature, which impose different levels of instability. The experiment was performed for two force directions. In addition to sessions in which objects of a particular curvature were presented repeatedly, we also measured the stiffness in sessions in which objects of different curvature were randomly interleaved. Importantly, the required force level generated by the subject against the objects was kept constant throughout the experiment so that any changes in stiffness are independent of the net force level. This allowed us to assess both the changes in the...
geometry of stiffness and the extent to which stiffness can be adapted from trial-to-trial to match varying task demands.

Materials and Methods

Experiment

Six healthy, right-handed subjects (ages 23–37 years) participated in the main study (four male, two female). Seven healthy, right-handed subjects (ages 22–37 years) participated in a second study. Five of these subjects completed both the main study and the second study. The institutional ethics committee approved the experiments, and the subjects gave informed consent before participating in the experiment. In the main study, subjects participated in two experimental sessions each of −1.5 h on separate days. The second study was performed in a single session of 1.5 h.

Apparatus. Subjects were seated in a sturdy chair (Saab seat) in front of a planar robotic device (vBOT) (Howard et al., 2009). Their shoulders were strapped against the backrest of the chair by a four-point seatbelt. The subjects’ right forearm was securely coupled to the vBOT handle by a custom-molded thermoplastic cuff (Omega Max/Plus; Promedics) that also immobilized the wrist joint. The forearm rested on an air sled that supported the weight of the arm. The vBOT handle and the vBOT arm. The vBOT was controlled at 1000 Hz. Joint angles, handle accelerations, and handle forces were sampled at the same frequency. Veridical feedback of the hand position and other task-relevant cues was provided by a projection from a monitor (Apple Cinema, 30 inches, 16 ms loop latency) in a mirror located just above the robot handle.

Experimental task. Subjects produced isometric forces against simulated rigid objects (Fig. 1). The hand position was continuously presented to the subject by a filled circle of 0.5 cm radius. The hand representation corresponded to the actual hand position except during the perturbations when the hand representation was frozen.

Trials were self-initiated by the subjects moving their hand into the start circle (Fig. 1A). The rigid object and force target (gray square) were then presented. When the hand contacted the object, the robot generated appropriate haptic feedback of the interaction forces. The force vector representing the force subjects exerted on the object was displayed (Fig. 1B, red arrow), and the subject was required to direct this force vector into the force target (Fig. 1C). The force target was a square with its closest boundary at 7.5 cm and sides of 2 cm. The force vector was drawn with a scale of 1 N = 1 cm requiring subjects to generate between 7.5 and 9.5 N. Whenever the tip of the force vector was within the target area, the force target turned from gray to white. Subjects were required to maintain the force vector continuously within the force target for a predefined time (1.5–2.5 s, randomly drawn from a uniform distribution), after which the hand position was perturbed as part of the stiffness estimation (Fig. 1D) (see section on stiffness estimation). To avoid subjects interpreting the perturbation onset as the end of a trial and moving back to the start region, they were required to maintain the force until the end of the perturbation. If they failed to do so, the start region would not appear until subjects had reproduced the desired force again.

Haptic force feedback of the hand–object interaction was simulated for a “cup” and three circular objects of different curvature [C = (4.00, 2.00, 0.67) cm⁻¹] (Fig. 1E). The hand–object interaction force was simulated with a stiff spring (90 N/cm), and the force was always perpendicular to the surface at the interaction point. No frictional forces parallel to the surface were simulated. This resulted in unstable interactions for the objects with positive curvature. The cup condition is fully stable, and we plot results as though this had a curvature of zero (although it is in fact more stable than a flat surface). This plotting convention does not affect any statistical tests.

The main experiment was split into two sessions performed on separate days. In this experiment, we looked at stiffness modulation while producing force in the negative x-direction (axes shown in Fig. 1). The subject’s position relative to the hand–object interaction point was adjusted such that the shoulder and elbow angles were 45° and 90°, respectively, and that the shoulders were parallel to the x-axis. After familiarization, subjects completed 120 trials for each object in each experimental session (480 trials/d). In one session, each of the four objects was presented in blocks of 120 trials in which the block order was randomized (“blocked”). In the other session, the objects were presented in random order, changing from trial to trial (“random”). Half of the subjects started with the blocked session and the remaining half with the random session. All six subjects participated in both the blocked and random sessions.

A second experiment was performed to investigate the modulation of stiffness while producing forces along the positive y-direction (axes

Figure 1. Overview of the experimental setup and paradigm for the main experiment. An additional experiment was performed with the visual and haptic scene rotated 90° clockwise. A, Visual display when the subject is not touching the rigid object. Orange half circle represents a simulated rigid object that is fixed in space. The square is the target area, and the purple circle is the veridical representation of the subject’s hand position. The hand is in the start area (black circle). The target area is gray, indicating that the force vector is not in it. B, Subject touches the rigid object and feels the interaction force. The force exerted on the object is shown to the subject as a red arrow. The start area is no longer presented. C, Same as above, but now the force vector is correctly within the target, which becomes white. D, After a 1.5–2.5 s delay, the visual display is frozen and the hand is moved 8 mm to one of eight positions around a circle (blue). The visual display, the perturbation positions, and the subject are not drawn on the same scale. E, The four objects with which the subjects interact. C stands for curvature with unit cm⁻¹. All objects had the same color in the experiment. The Cartesian axes are indicated by x and y, and the shoulder and elbow joint angles are indicated by θ₁ and θ₂.
shown in Fig. 1). In this experiment, targets were only presented in blocks. The subject’s position relative to the hand–object interaction point was adjusted such that the shoulder and elbow angles were 30° and 80°, respectively. For this experiment, the required endpoint force range was decreased to 6.5–8.5 N. All other parameters of the experiment were the same as in the main experiment.

Task performance. Task performance was quantified with two measures. First, the time it took a subject to finish a trial, defined as the time the hand was in contact with the object before the force vector entered into the target for the final occasion (because it was possible to slip out of the target or off the object) was recorded. Second, for each trial, the mean force vector from 500 to 1500 ms after entering the force target was calculated.

Stiffness estimation. After the force vector was maintained within the force target for the predefined minimal time (1.5–2.5 s), the robot switched from force to position servo control (position gain, 120 N/cm; velocity gain, 0.8 Ns/cm). The servo smoothly and rapidly displaced the hand to one of eight equally distributed positions on a circle of 8 mm radius centered on the hand position just before perturbation onset (Fig. 1D). To avoid any visually induced reactions, visual feedback was frozen during the perturbations. The displacement consisted of a smooth 80 ms ramp-away, a 300 ms hold, and a 120 ms ramp-back period. The average restoring force and displacement between 170 and 230 ms after perturbation onset were used to estimate the two-by-two endpoint stiffness matrix \( K \) by linear regression:

\[
\Delta F_x = \begin{bmatrix} K_{xx} & K_{xy} \\ K_{yx} & K_{yy} \end{bmatrix} \Delta p_x,
\]

where \( \Delta P_x \) indicates the mean change measured in the perturbed location with respect to the mean measured in the final 300 ms before perturbation. The endpoint stiffness can be represented as an ellipse (Mussa-Ivaldi et al., 1985). Singular value decomposition of the stiffness matrix \( K \) was used to determine the area, shape, and orientation of the stiffness ellipses (Gomi and Osu, 1998). Statistics. All data analyses were performed offline in Matlab (MathWorks). Statistical analyses were performed using general linear models (SPSS). Most statistical analyses were repeated-measures ANOVAs with object curvature \( C \) in SPSS 16.0 (SPSS). Most statistical analyses were repeated-measures ANOVAs with object curvature \( C \) in SPSS 16.0 (SPSS). Most statistical analyses were repeated-measures ANOVAs with object curvature \( C \) in SPSS 16.0 (SPSS). Most statistical analyses were repeated-measures ANOVAs with object curvature \( C \) in SPSS 16.0 (SPSS).

Model

Theoretical aspects of stiffness geometry on force and position variability. To understand the mechanisms by which force variability and stiffness interact during haptic interactions, a simple musculo–skeletal model of our task was built. For simplicity, the model only captures the open-loop behavior of the system and does not model reflexive and visual contributions. Simulations of this model were used to investigate the qualitative effects of endpoint stiffness geometry on force variability and position variability. Both instances of variability are the result of the signal dependency of the force fluctuations of the individual muscles (Harris and Wolpert, 1998; Jones et al., 2002), mediated by the dynamics, including the stiffness, of the musculoskeletal system (Selen et al., 2005). The arm was modeled as a two-link system exerting a force of 7.5 N onto a rigid circular object. The circular object had no surface friction. The arm model was driven by six muscles: four mono-articular muscles, two crossing the elbow and two crossing the shoulder, and two bi-articular muscles.

The force attributed to each muscle was derived from the required endpoint stiffness matrix and external force demand. The stiffness geometry of the endpoint arm can be expressed as an endpoint stiffness matrix \( K \) in Cartesian space:

\[
K = \begin{bmatrix} K_{xx} & K_{xy} \\ K_{yx} & K_{yy} \end{bmatrix}.
\]

For our simulations, we set \( K_{xx} = K_{yy} \) equal, resulting in a purely conservative stiffness (Mussa-Ivaldi et al., 1985) as was observed in the experiments. From the endpoint stiffness, the joint stiffness \( R \) can be determined (McIntyre et al., 1996):

\[
R = J^T K J + \frac{\partial J^T K}{\partial \alpha} F,
\]

where \( J \) represents the Jacobian matrix of the current limb configuration, and \( \alpha \) represents the joint angles. The second term describes the geometric stiffness, which is a tensor product between the derivative of the Jacobian matrix \( J \) and the endpoint force \( F \). This term corrects for the change in endpoint force when the hand is moved slightly and the net joint torques remain the same. The joint stiffness results from the stiffness of the individual muscles:

\[
R = D^T MD
\]

where \( D \) is a \( 6 \times 2 \) matrix of the moment arms of the muscles around the shoulder and elbow joint. Moment arms were defined positive for flexor muscles and negative for extensor muscles and based on published values (Murray et al., 1995; Kuechle et al., 1997; Nijhof and Kouwenhoven, 2000) (for model parameters, see Table 1). \( M \) is a diagonal matrix representing the stiffness of each muscle, at which the muscle stiffness terms \( M_{m,m} \) depend on the muscular force \( F_m \):

\[
M_{m,m} = c_m F_m
\]

The scaling constant \( c_m \) was based on published joint torque stiffness (Gomi and Osu, 1998; Franklin and Milner, 2003) and muscle force stiffness (Edman and Josephson, 2007) regressions. We show results for \( c_m = 75 \text{ m}^{-1} \) across all muscles, but results look similar for other values within the physiological range. Combining these equations gives the following:

\[
K = (J^T)^{-1} \left( D^T \text{diag}(c_m F_m) D + \frac{\partial J^T}{\partial \alpha} F \right) J^T.
\]

To calculate the muscle forces from the endpoint stiffness, we use the additional constraint that the joint torques \( \mathbf{T} \) create the desired endpoint force:

\[
\mathbf{T} = D^T \hat{\mathbf{F}}
\]

Both of these equations were simultaneously solved with the additional constraint that the sum of the squared muscular forces was minimized. This criterion was taken as a heuristic for energy expenditure. With a six-muscle arm model, only a limited range of stiffness matrices can be created.

The muscle forces resulting from the optimization were subsequently contaminated with SDN and smoothed with a second-order filter with time constants of 30 and 40 ms. The amount of SDN [coefficient of variation (CV) = 0.15] was chosen so that the CV of the filtered force traces was 3% (Hamilton et al., 2004; Moritz et al., 2005). Note that using lower CV values that have been suggested for the more proximal joints (Hamilton et al., 2004) does not affect the basic result of the simulation. In a forward simulation, these noisy forces were exerted on a two-link system with the corresponding joint stiffness matrix and external con-
strains set by the object curvature. The joint damping matrix was set equal to 5% of the stiffness matrix. This value is of similar magnitude to both that used in computational models of the arm (Franklin et al., 2008) and those measured experimentally (Dolan et al., 1993; Perreault et al., 2004). Outcome measures were the force variability and the kinematic variability of the endpoint of the system over a 10 s simulation. Both $K_{xx}$ and $K_{yy}$ varied from 100 to 600 N/m and the off-diagonal elements $K_{xy}$ and $K_{yx}$ from 0 to 200 N/m. Simulations were performed for object curvatures of 0.01, 0.1, 0.2, and 0.4 cm$^{-1}$. For our model, we took a force to stiffness ratio that was based on relatively large perturbations and therefore we probably underestimate the stiffness (Kearney and Hunter, 1982; Shadmehr et al., 1993). Because of this, the lack of active feedback mechanisms, our model becomes unstable during interactions with objects of higher curvature.

Intrinsic and reflexive contributions to impedance. For simplicity, the model only attempts to predict the open-loop behavior of the limb and does not include feedback contributions. It is clear that reflex pathways significantly contribute to muscle stiffness (Nichols and Houk, 1976; Hoffer and Andreassen, 1981; Carter et al., 1990) and are modulated with task (Nashner 1976; Akazawa et al., 1983; Lacquaniti et al., 1991; Bennett et al., 1994) and environmental dynamics (Franklin et al., 2007; Damm and McIntyre, 2008; Perreault et al., 2008; Pruszynski et al., 2008). Despite this evidence, we have chosen to model only the open-loop behavior of the limb. This is because we are not yet able to accurately model the reflex contributions to the impedance control during natural tasks. The only current techniques that allow for simultaneous estimates of both intrinsic and reflex stiffness either have not yet been applied to the two-joint limb because of limitations of current robotic devices (Stein and Kearney, 1995) or require stochastic perturbations that disturb performance of a natural task (Kearney et al., 1997; Zhang and Rymer 1997; Perreault et al., 2000; van der Helm et al., 2002). This means that any modeled reflex contributions to the control of impedance would be physiologically unconstrained. Such modeling would not allow us to accurately understand the interplay between noise and stiffness. Our modeling therefore focused purely on the modulation of the intrinsic stiffness to see whether this portion of the controlled impedance could explain the rather surprising experimental results. By constraining our model in this manner, we gained understanding of the interplay between muscle stiffness, environmental instability, and SDN.

**Results**

**Forces**

**Buildup**

Building up the required force while maintaining stability took time. As object curvature increased, this force buildup time increased fourfold (main study, $F_{(3,15)} = 33.371, p < 0.001$; second study, $F_{(3,18)} = 19.543, p = 0.002$) (Fig. 2A). Force buildup times were not significantly different between the blocked or random sessions, and neither was there a significant interaction between object type and session. Several mechanisms may be responsible for the slower buildup; force variability tends to decrease with decreasing speed (Gordon and Ghez, 1987), and higher forces take more time to build up and are needed to increase the stiffness (Edman and Josephson, 2007).

**Hold phase**

After the buildup, subjects were required to keep the interaction force, represented by the force vector, within a target window of 7.5 to 9.5 N for at least 1.5 s before a perturbation occurred and the trial finished. Subjects exploited this force margin by lowering the average length of the force vector as the object curvature increased (main study, $F_{(3,15)} = 27.930; p < 0.001$; second study, $F_{(3,18)} = 8.463, p = 0.001$) (Fig. 2B), thereby possibly reducing the SDN in the force signal. The average length of the force vector did not differ between blocked and random sessions. However, a significant interaction between object curvature and session type was found ($F_{(3,15)} = 5.581, p = 0.009$).

Post hoc repeated measures on the sessions separately showed that the length of the force vector decreased with increasing object curvature for both sessions (blocked, $F_{(3,15)} = 19.067, p < 0.001$; random, $F_{(3,15)} = 14.331, p < 0.001$). Subsequently, we performed post hoc paired $t$ tests between the sessions for the individual objects. For the cup condition, the length of the average force vector was significantly smaller in the random than in the blocked session ($p = 0.048$). These results suggest that subjects reduce the force produced as the task becomes harder. Bringing the magnitude of the force vector closer to the lower boundary of the target force area increases the risk of producing too little force, thereby resetting the hold phase timer. However, this strategy is still less costly than slipping off the object. In the former case, the force does not have to be built up again from zero but only has to be increased by a small amount to get into the target area again.

**Stiffness**

The endpoint stiffness was estimated using linear regression of the force and position traces for the final 80 trials for each object. The regression was performed on the time-averaged force and position in the estimation window (170–230 ms) of all individual perturbation trials. The variance explained ($r^2$) by this linear regression ranged from 0.89 to 0.98 over all the subjects, force directions, objects, and sessions.

**Main study**

Figure 3A presents the stiffness ellipses for the force in negative $x$-direction for all subjects, object curvatures, and experimental sessions. The size of the stiffness ellipse (Fig. 3B), a measure of the global increase in stiffness, systematically increased with increasing object curvature ($F_{(3,15)} = 69.613, p < 0.001$). The stiffness ellipses systematically rotated toward the direction of instability (Fig. 3C) with increasing object curvature ($F_{(3,15)} = 23.869, p < 0.001$). However, this rotation was small (maximum rotation, 23°), and the orientation of the ellipse never fully reached the 90° direction of the instability (closest value, 110°).

The stiffness ellipse, its size, and orientation are convenient measures to represent the characteristics of the stiffness matrix. However, the full information about the endpoint stiffness is contained in the elements of the stiffness matrix (Fig. 4A). The diagonal elements $K_{xx}$ and $K_{yy}$ increased with increasing object curvature. The off-diagonal elements $K_{xy}$ and $K_{yx}$ increased with increasing object curvature.
curvature $(F_{3,15} = 12.234, p < 0.001; F_{3,15} = 61.511, p < 0.001)$. Across all objects, no significant main effect was observed between the blocked and random session for any element of the stiffness matrix. However, an interaction between object and session was found for $K_{yy}$ $(F_{3,15} = 4.897, p = 0.014)$. To study this further, pairwise comparisons of $K_{yy}$ between the blocked and random sessions for the individual objects were performed, showing that, for the lowest curvature and the cup condition, $K_{yy}$ was higher in the random compared with the blocked session ($p = 0.013$ and $p = 0.050$). The ratio of $K_{yy}/K_{xx}$ was calculated to further examine the modulation of the total stiffness. This ratio increased with object curvature $(F_{3,15} = 36.603, p < 0.001)$, indicating that $K_{yy}$ increases faster than $K_{xx}$.

Second study

Stiffness ellipses for the individual subjects and the elements of the endpoint stiffness matrix are presented in Figure 5 for forces in the positive y-direction. For this direction, the modulation of the stiffness ellipse with object curvature is much more variable between subjects (Fig. 5A). However, across all subjects, only the modulation in $K_{xx}$ reaches significance with object curvature $(F_{3,15} = 9.439, p = 0.014)$ (Fig. 5B). Also for this force direction, the ellipses are, in general, not oriented along the instability direction, and the off-diagonal elements of the stiffness matrix did not vary with curvature, remaining at approximately −120 N/m (Fig. 5B).

Rancourt and Hogan (2001) have performed theoretical analyses on the stability requirements for a push-on-a-stick paradigm, which is mathematically equivalent to our experiments: the hand representation, together with the curved object, can be described as a pivoting stick around the center of the curved object. In the case of our main experimental task, theoretical values of $K_{yy}$ should be >1500, 1000, 428, and 0 N/m, respectively. Several factors may have contributed to the lower stiffness estimates in our experiment. First, our stiffness estimates were based on relatively large perturbations (8 mm) compared with the infinitely small perturbations for the theoretical derivations. Previous studies have demonstrated that muscle (Rack and Westbury, 1974; Kearney and Hunter, 1982; MacKay et al., 1986) and limb (Shadmehr et al., 1993) stiffness decreases nonlinearly with the amplitude of the perturbations used for stiffness estimation, resulting in stiffness underestimates for larger perturbations. Another possible explanation for measured stiffness values lower than the theoretical values could be that the hand is not locally stable (Hasan, 2005) but relies on corrective responses for compensation. The feedback mechanisms necessary for these corrective responses are not taken into account in neither the mathematical derivations by Rancourt and Hogan (2001) nor our simulations. Finally, the robotic manipulandum has some static and dynamic friction that adds to the overall stability of the system and reducing the required stiffness of the arm. Nevertheless, with these lower stiffness values, our subjects were able to stabilize their hand while pushing.

History dependence of the stiffness matrix

Previous studies have shown that motor actions in the current trial systematically depend on the history of previous trials for grip force modulation (Witney et al., 2001), force compensation (Scheidt et al., 2001), and EMG modulation (Osu et al., 2002; Franklin et al., 2008) during motor adaptation to novel force fields. Our observation, in the main experiment, that the endpoint stiffness was higher in the random compared with the blocked session for the more stable objects similarly suggests that the endpoint stiffness in the previous trial(s) is not entirely washed out during the force buildup of the present trial. To further investigate this, we calculated the stiffness ellipse for all possible trial transitions to all objects and compared that with the average stiffness for that object. For example, to examine the influence of the previous trial on the stiffness estimate for the object of curvature 2, we calculated the stiffness for the following transitions: curvature
Our main experiment, in which forces were produced in negative x-direction, showed two surprising results. First, subjects modulated their stiffness not only in the direction of the instability (the y-direction) but also in the orthogonal direction. Second, the orientation of the stiffness ellipse was never in the direction of the instability and $K_{yy}$ remained approximately constant. These findings are at odds with studies on reaching movements in unstable environments, in which the major axis of the stiffness ellipse is oriented in the direction of instability (Burdet et al., 2001; Franklin et al., 2003b, 2007) and only modulates in that direction (Franklin et al., 2004). We hypothesized that our findings could arise because to maintain stability the motor system has to trade off the stabilizing properties of stiffness and the destabilizing properties of noise and that this tradeoff will depend in a complex way on the task geometry.

To investigate this, we simulated the effects of different stiffness geometries on force and position variability in a simple planar arm model. All attainable stiffness geometries for a stiffness-to-force constant of 75 m$^{-1}$ were derived (see Materials and Methods). The muscle forces required to generate the stiffness geometry were contaminated with SDN with a CV of 3%.

Figure 7 shows how different stiffness geometries and object curvatures affect the kinematic variability (expressed as SD) of the endpoint of the arm. $K_{yy}$ is varied along the columns and object curvature along the rows. Note that the object curvatures are smaller than those in the experiments. Presumably because of the lack of visual and reflexive feedback, our model could not maintain stability for objects of curvatures above 0.4 cm$^{-1}$. The top row of Figure 7 shows the kinematic variability when the endpoint of the arm pushes onto a frictionless wall. The valley of minimal variability, shown in white, is a function of both $K_{xx}$ and $K_{yy}$, and it is along this valley that stiffness will be modulated. To reduce kinematic variability, subjects will have to change their stiffness geometry along this manifold and increase $K_{xx}$ and $K_{yy}$ simultaneously. Furthermore, it is clear that more negative $K_{yy}$ values result in less kinematic variability and a broader region, i.e., a shallower valley, of low kinematic variability. As object curvature increases, along the rows of Figure 7, the kinematic variability for the same stiffness geometry increases (note the different color bar scales). The region spanned by $K_{xx}$ and $K_{yy}$ combinations reduces because, for certain combinations, the hand slips off the object.

These simulations, therefore, suggest that both $K_{xx}$ and $K_{yy}$ have to be increased for stability. In addition, they provide indications why we found experimentally that subjects have a constant, non-zero, off-diagonal term ($K_{xy}$) in the stiffness matrix at all times: for a given combination of $K_{xx}$ and $K_{yy}$, more negative values of $K_{xy}$ are associated with lower global energy demands, expressed as the sum of all muscular forces (Fig. 8). However, lowering $K_{xy}$ even further may be suboptimal because this requires extensive activation of the mono-articular shoulder muscles, thereby increasing the local physiological cost (Fig. 9, dashed lines).

In contrast to the main experiment, for the second experiment (positive y-direction), significant modulation of only $K_{xx}$ was observed. We also simulated the effects of different stiffness geometries on position variability for this task. In correspondence with the experimental result, position variability was hardly influenced by changes in $K_{yy}$ resulting in the absence of a clear valley of minimum position variability (Fig. 10B). Furthermore, the model predicts that position variability decreases with increasing

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**Figure 4.** Changes in the endpoint stiffness matrix for forces in the main study (negative x-direction). A. The mean ± SEM elements of the endpoint stiffness matrix. Circles indicate the blocked session and squares the random session. Both $K_{xx}$ and $K_{yy}$ show a significant increase with object curvature, and $K_{xy}$ differed between the blocked and random sessions for the cup and lowest curvature conditions. B. Changes in the ratio of $K_{xx}$ and $K_{yy}$ of the stiffness matrix. $K_{xx}/K_{yy}$ differed between the blocked and random session for the cup and lowest curvature conditions.

4.00 $\rightarrow$ curvature 2.00, curvature 2.00 $\rightarrow$ curvature 2.00, curvature 0.67 $\rightarrow$ curvature 2.00, cup $\rightarrow$ curvature 2.00.

Repeated-measures ANOVA with four possible transitions toward four possible objects revealed significant effects of both transition ($F_{3,21} = 5.343, p = 0.007$) and object ($F_{3,21} = 27.235, p = 0.001$) on $K_{yy}$. Because there were no interactions, we collapsed the transition data for all object curvatures (Fig. 6A).

Interacting with the object of curvature 4 on the previous trial will on average result in stiffness for the present trial that is 20 N/m higher than the average stiffness for the object of the present trial. Similarly, having interacted with the cup object in the previous trial will lower the stiffness in the present trial by approximately 10% of the stiffness change can be explained by the curvature of the object on the previous trial.

**Theoretical aspects of stiffness modulation for stabilization in a force production task**

Our main experiment, in which forces were produced in negative x-direction, showed two surprising results. First, subjects modulated their stiffness not only in the direction of the instability (the y-direction) but also in the orthogonal direction. Second, the orientation of the stiffness ellipse was never in the direction of the instability and $K_{yy}$ remained approximately constant. These findings are at odds with studies on reaching movements in unstable environments, in which the major axis of the stiffness ellipse is oriented in the direction of instability (Burdet et al., 2001; Franklin et al., 2003b, 2007) and only modulates in that direction (Franklin et al., 2004). We hypothesized that our findings could arise because to maintain stability the motor system has to trade off the stabilizing properties of stiffness and the destabilizing properties of noise and that this tradeoff will depend in a complex way on the task geometry.

To investigate this, we simulated the effects of different stiffness geometries on force and position variability in a simple planar arm model. All attainable stiffness geometries for a stiffness-to-force constant of 75 m$^{-1}$ were derived (see Materials and Methods). The muscle forces required to generate the stiffness geometry were contaminated with SDN with a CV of 3%.

Figure 7 shows how different stiffness geometries and object curvatures affect the kinematic variability (expressed as SD) of the endpoint of the arm. $K_{yy}$ is varied along the columns and object curvature along the rows. Note that the object curvatures are smaller than those in the experiments. Presumably because of the lack of visual and reflexive feedback, our model could not maintain stability for objects of curvatures above 0.4 cm$^{-1}$. The top row of Figure 7 shows the kinematic variability when the endpoint of the arm pushes onto a frictionless wall. The valley of minimal variability, shown in white, is a function of both $K_{xx}$ and $K_{yy}$, and it is along this valley that stiffness will be modulated. To reduce kinematic variability, subjects will have to change their stiffness geometry along this manifold and increase $K_{xx}$ and $K_{yy}$ simultaneously. Furthermore, it is clear that more negative $K_{yy}$ values result in less kinematic variability and a broader region, i.e., a shallower valley, of low kinematic variability. As object curvature increases, along the rows of Figure 7, the kinematic variability for the same stiffness geometry increases (note the different color bar scales). The region spanned by $K_{xx}$ and $K_{yy}$ combinations reduces because, for certain combinations, the hand slips off the object.

These simulations, therefore, suggest that both $K_{xx}$ and $K_{yy}$ have to be increased for stability. In addition, they provide indications why we found experimentally that subjects have a constant, non-zero, off-diagonal term ($K_{xy}$) in the stiffness matrix at all times: for a given combination of $K_{xx}$ and $K_{yy}$, more negative values of $K_{xy}$ are associated with lower global energy demands, expressed as the sum of all muscular forces (Fig. 8). However, lowering $K_{xy}$ even further may be suboptimal because this requires extensive activation of the mono-articular shoulder muscles, thereby increasing the local physiological cost (Fig. 9, dashed lines).

In contrast to the main experiment, for the second experiment (positive y-direction), significant modulation of only $K_{xx}$ was observed. We also simulated the effects of different stiffness geometries on position variability for this task. In correspondence with the experimental result, position variability was hardly influenced by changes in $K_{yy}$ resulting in the absence of a clear valley of minimum position variability (Fig. 10B). Furthermore, the model predicts that position variability decreases with increasing
before reaching a minimum at $K_{xy}$ before reaching a minimum at $-120$ N/m. This value nicely corresponds with the experimental observations.

Figure 10 summarizes and relates the experimental and simulation results for both studies. Our simple arm model predicts a strong dependence between $K_{xx}$ and $K_{yy}$ for the negative $x$-force direction of the main study (Fig. 10 A), resulting in a valley along which to modulate stiffness. Because the orientation of this valley hardly depends on object curvature (Fig. 7), we show results for a simulated wall. In addition, we fixed $K_{xy}$ to $-150$ N/m, which corresponds with our experimental findings. As stated previously, $K_{xy}$ hardly influences the kinematic variability in the simulations for the second study; positive $y$-direction (Fig. 10 B). To summarize the experimental findings, we calculated the linear regression for all observed pairs of $K_{xx}$ and $K_{yy}$ (Fig. 10 C). The regression slope is not different from zero for the second study (positive $y$-force direction), whereas the slope for the main study (negative $x$-force direction) is significant (slope = 1.66, $p = 0.007$) and similar to that of the valley derived from our simulations (slope = 1.52). We also show the mean and SEM for the individual object curvatures and the two force directions.

In conclusion, we found an increase in both $K_{xx}$ and $K_{yy}$ for the main study (negative $x$-force direction) and only an increase of $K_{yy}$ in the second study (positive $y$-force direction). Furthermore, for both studies, the stiffness matrix was never oriented along the instability axis. These results are explained by the model as a tradeoff between adding stiffness to maintain stability and minimizing the detrimental effects of SDN for which added stiffness does not compensate.

Discussion

In this study, we investigated the ability of the neuromuscular system to control the endpoint stiffness of the arm in an unstable force production task. As the curvature of the objects increased (higher instability), subjects changed their endpoint stiffness, in both the overall size and orientation. In particular, subjects adapted their arm endpoint stiffness geometry predominantly in the direction of the instability but also in the orthogonal direction. Simulations showed that these features represent a tradeoff between stability engendered by the increase in stiffness and the destabilizing effects of neuromotor noise. Random presentation of object curvatures resulted in a clear influence of the object curvature in the preceding trial on the endpoint stiffness in the current trial.

Influence of SDN on stiffness geometry

Our findings complement previous studies in which energy was added to the system to create an unstable environment. Increased instability during movement, caused by an external divergent force field, resulted in an alignment of the stiffness geometry with the direction of instability (Burdet et al., 2001; Franklin et al.,
2003b, 2007) and scaled with the magnitude of the instability (Franklin et al., 2004). During posture maintenance, the addition of energy, in the form of directional force pulses, resulted in changes of the stiffness geometry that were specific to the instability of the environment (Darainy et al., 2004). In contrast, our study examined natural interactions in which instability arises from purely passive elements in the world and noise in the motor commands.

We found only limited changes in the orientation of the endpoint stiffness as the object curvatures increased, with a maximum change of 23° and the closest ellipse orientation to the 90° instability direction being 110°. Similar small changes in the ellipse orientation have been reported previously for postural tasks (Perreault et al., 2002; Darainy et al., 2004). However, the orientation of the stiffness ellipse itself is less important than the change in the endpoint stiffness relative to the normal endpoint.

Figure 7. The simulated variability of endpoint position in relation to the endpoint stiffness and task geometry for the main study. Endpoint variability is caused by SDN on the muscular forces. Each panel depicts the kinematic variability (SD) as a function of $K_{xx}$ and $K_{yy}$. The columns represent different off-diagonal terms of the stiffness matrix ($K_{xy}$), with the leftmost column showing all stiffness geometries having one of their axes along the instability direction. Task geometry is expressed as object curvature, which increases down the rows ($C = 0, 0.1, 0.2, 0.4 \text{ cm}^{-1}$). The kinematic variability results for each object curvature are plotted using different scales as indicated beneath each row. Note that, with increasing curvature, the kinematic variability increases, which for some stiffness geometries results in slip offs. This is reflected by the increase of the white area. White lines indicate the valley of kinematic variability minima (i.e., the $K_{xx}$ that minimizes the kinematic variability for a given $K_{yy}$).
stiffness. This was examined with the changes in the $K_{xx}$ and $K_{yy}$ terms of the stiffness matrix. Whereas the ratio of $K_{yy}/K_{xx}$ increased with object curvature, indicating that the greatest change in the endpoint stiffness was in the direction of the instability, both $K_{yy}$ and $K_{xx}$ increased as this instability increased. Therefore, the endpoint stiffness of the arm increased in both the direction of the instability and the orthogonal force direction.

Based on numerical simulations, it has been argued that the properties of the neuromuscular system limits rotation of the stiffness ellipse to this small range (Darainy et al., 2004). In contrast, our numerical simulations indicated that, in principle, the neuromuscular system could orient the major axis of the stiffness ellipse in the direction of the instability (Fig. 5, left column) ($K_{yy} = 0$). This ability arises in our model because, unlike the previous model, we allowed the independent control of coactivation of monoarticular and bi-articular muscles. Although previous studies of stable force control tasks have shown mainly changes in the single joint muscles (Perreault et al., 2001) or a combined control over both the single and bi-articular muscles (Gomi and Osu, 1998), studies of unstable environments have favored a unique role for the bi-articular muscles (McIntyre et al., 1996) and independent control over these muscles for stability purposes (Franklin and Milner, 2003; Franklin et al., 2003a, 2007). Additional support for this has been seen in the relative changes in bi-articular muscle involvement between force and movement control (Tax et al., 1990; van Groeningen and Erkelens, 1994; van Bolhuis and Gielen, 1997). These studies suggest that there is at least a degree of independent control over the mono-articular and bi-articular muscles that could lead to a greater degree of control over the endpoint stiffness than was predicted previously.

However, the most important finding of the simulation was that the lowest kinematic variability was not obtained when the stiffness ellipse was oriented in the direction of the instability. Instead, it was obtained when the model adapted to the instability in a similar pattern to that observed in our subjects, with both an increase in the $K_{xx}$ and $K_{yy}$ terms of the stiffness matrix and only
on the endpoint stiffness itself. We argue that the neuromuscular system may be able to rotate the stiffness ellipse over a wider range than has been shown previously in static studies but that an additional rotation toward the instability direction is suboptimal when one considers the effects of SDN. For both force production directions, our simulations show that SDN has a bigger effect on kinematic variability when the main axis of the stiffness ellipse is along the instability direction. Having non-zero off-diagonal terms in the stiffness ellipse reduces this influence, thereby guaranteeing stability. These non-intuitive effects suggest that there are fundamental differences between the control of endpoint stiffness for movement variability reduction and for stabilization against external force fields.

Based on an unstable task requiring the compressing of a spring able to buckle, it has been argued that stiffness modulation is inconceivable to guarantee stability because it would introduce instability attributable to SDN (Venkadesan et al., 2007). The present study contradicts this claim and underpins previous simulation work (Selen et al., 2005), by showing that the increase in SDN at the muscular force level can be counteracted by increase in joint and endpoint stiffness. Nevertheless, it is conceivable that not all unstable interactions with the environment can be stabilized by stiffness modulation. In addition to changing the stiffness geometry, our subjects also exploited the size of the target force region to maintain stability. Lowering the forces has a positive effect on stability in two ways. First, the required stiffness decreases linearly with the average force (Rancourt and Hogan, 2001), and second, the perturbing forces attributable to SDN also decrease with lower forces (Jones et al., 2002; Hamilton et al., 2004).

The time course of stiffness modulation
When faced with a new dynamical environment, the CNS has to update its internal representation of (the stability of) that environment and adapt its control policy accordingly (Franklin et al., 2008). Because excessive coactivation is energy consuming (Franklin et al., 2004), it is expected that the CNS can quickly adapt the stiffness geometry to the instability of the environment. However, so far the buildup of this stability representation and the adaptation of the control policy have only been investigated over the time course of repeated trials with the same instability (Franklin et al., 2003b, 2004). The results of the present study suggest that the modification of the endpoint stiffness not only takes place between trials but may also take place as an online process within a trial. The longer force buildup times for the more curved objects suggest that modification of the endpoint stiffness may be an online process that is, at least partially, feedback driven.

Apart from this stiffness adaptation during the trial, we also found indications for a stiffness memory across trials. First, for the object of highest curvature, all stiffness measures were similar for the blocked and random sessions. However, the slope with which the total stiffness and $K_{yy}$ decreased with decreasing object curvature was lower for the random session, ultimately resulting in higher total stiffness and $K_{yy}$ for the cup and object of lowest curvature. This presumably is a reflection of the stiffness adaptation process that progresses over trials. Second, in the random session, there was a systematic effect of the previous trial on the observed stiffness in the present trial. Such effects have been reported previously in terms of EMG (Franklin et al., 2008) or the force (Scheidt et al., 2001) while learning a new force field but not on the endpoint stiffness itself.

Stiffness control for self-generated instability and noise
The present study experimentally confirms that stiffness geometry is adapted to the instability experienced in an isometric force production task. Increasing the stiffness of the limb requires larger muscle activation, which further results in larger force variability attributable to SDN (Jones et al., 2002; Hamilton et al., 2004). This force variability results in movement variability (Harris and Wolpert, 1998) that can be controlled by changing the stiffness geometry (Lametti et al., 2007) and magnitude (Selen et al., 2006a,b). Although some researchers have shown that force variability increases with co-contraction (Christou et al., 2007), our results show that this does not necessarily increase kinematic variability. In conclusion, although stiffness control is not a suitable solution for reducing force variability, it can reduce kinematic variability during interactions with objects.

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